

```
In[1]:= Clear[F, GradF2D, GradF]
```

```
In[2]:= F[x_, y_, z_] := 1 / Sqrt[x^2 + y^2 + z^2]
```

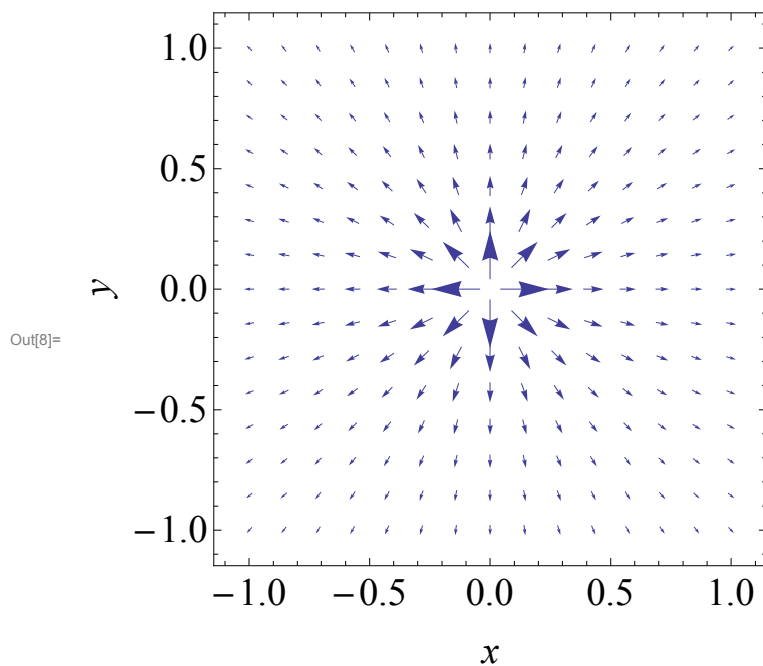
```
In[6]:= GradF2D[x_, y_] := Evaluate[-D[F[x, y, 0], {{x, y}}]]
```

(* Evaluate is required to distinguish dummy variables for D with dummy variables for GradF2D *)

```
In[7]:= GradF2D[x, y]
```

$$\text{Out[7]} = \left\{ \frac{x}{(x^2 + y^2)^{3/2}}, \frac{y}{(x^2 + y^2)^{3/2}} \right\}$$

```
In[8]:= VectorPlot[GradF2D[x, y], {x, -1, 1}, {y, -1, 1},  
VectorScale -> {Automatic, Medium, If[#5 > 100, 0, #5^0.4] &}, (* #5 is Norm *)  
BaseStyle -> {FontSize -> 20}, FrameLabel -> {x, y}]
```

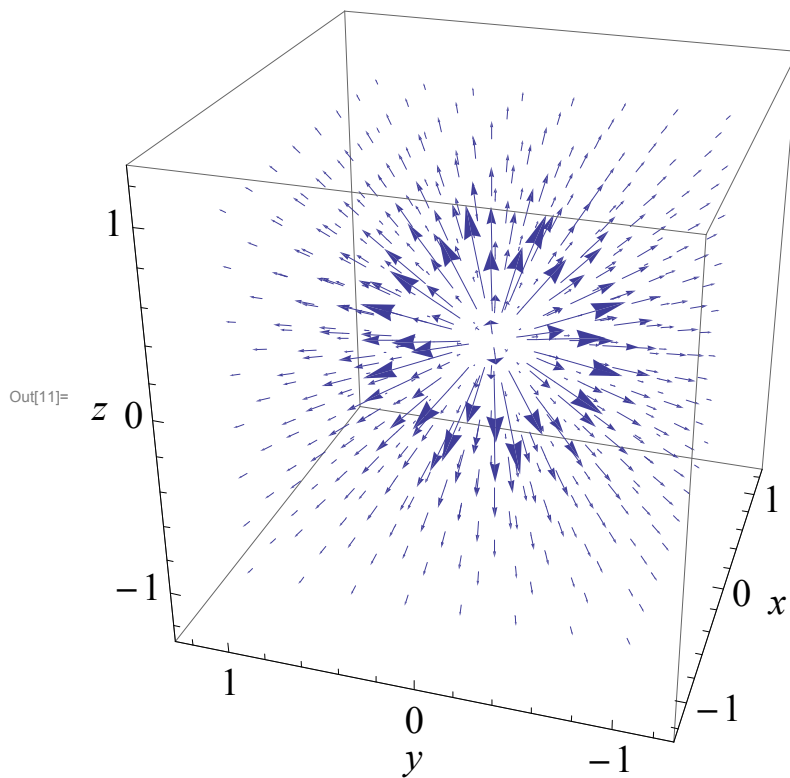


```
In[9]:= GradF[x_, y_, z_] := Evaluate[-D[F[x, y, z], {{x, y, z}}]]
```

```
In[10]:= GradF[x, y, z]
```

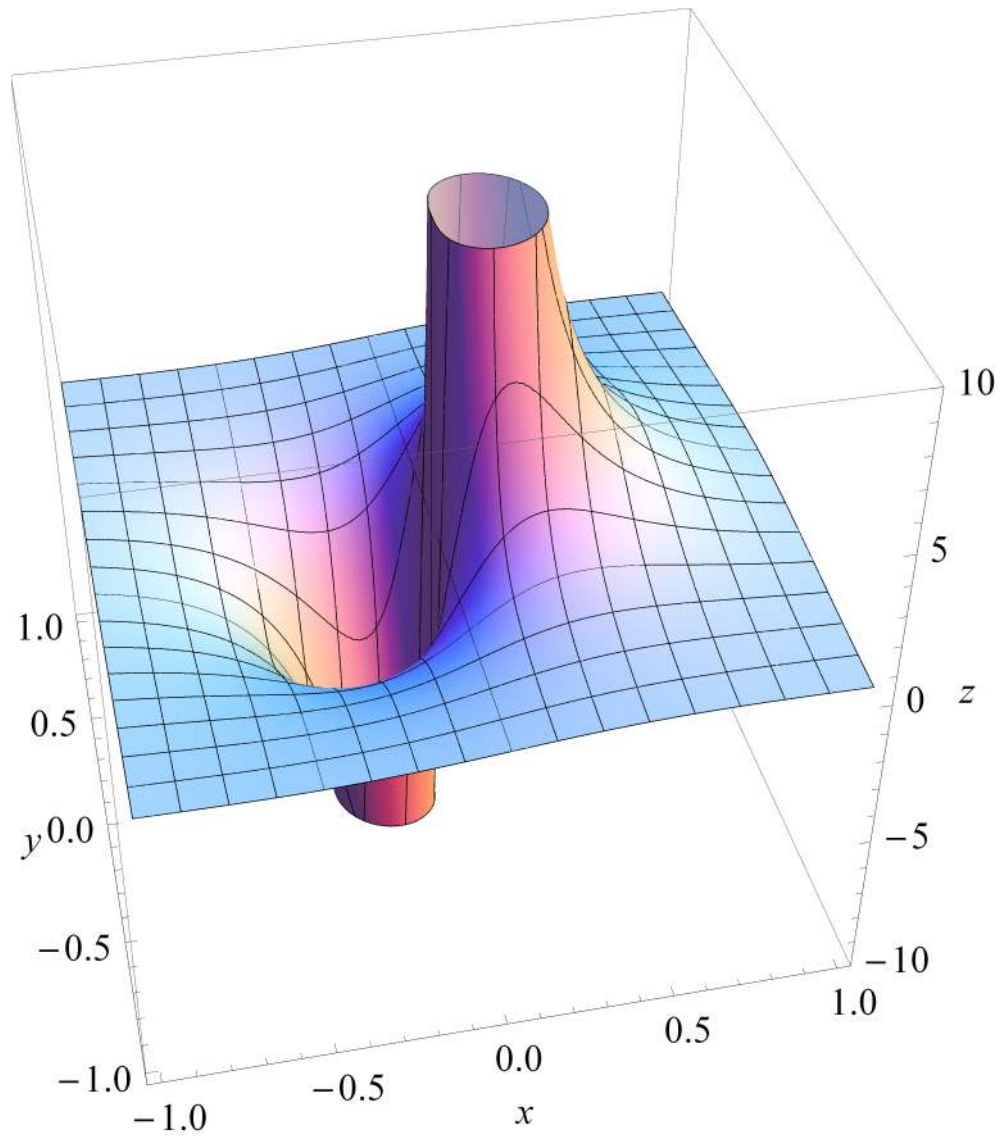
$$\text{Out[10]} = \left\{ \frac{x}{(x^2 + y^2 + z^2)^{3/2}}, \frac{y}{(x^2 + y^2 + z^2)^{3/2}}, \frac{z}{(x^2 + y^2 + z^2)^{3/2}} \right\}$$

```
In[11]:= VectorPlot3D[  
  If[ Norm[GradF[x, y, z]] > 10, {0, 0, 0}, GradF[x, y, z]],  
  {x, -1, 1}, {y, -1, 1}, {z, -1, 1},  
  VectorScale -> {Automatic, Small, Automatic},  
  (* #7 is expected to be Norm but not *)  
  BaseStyle -> {FontSize -> 20}, AxesLabel -> {x, y, z}]
```

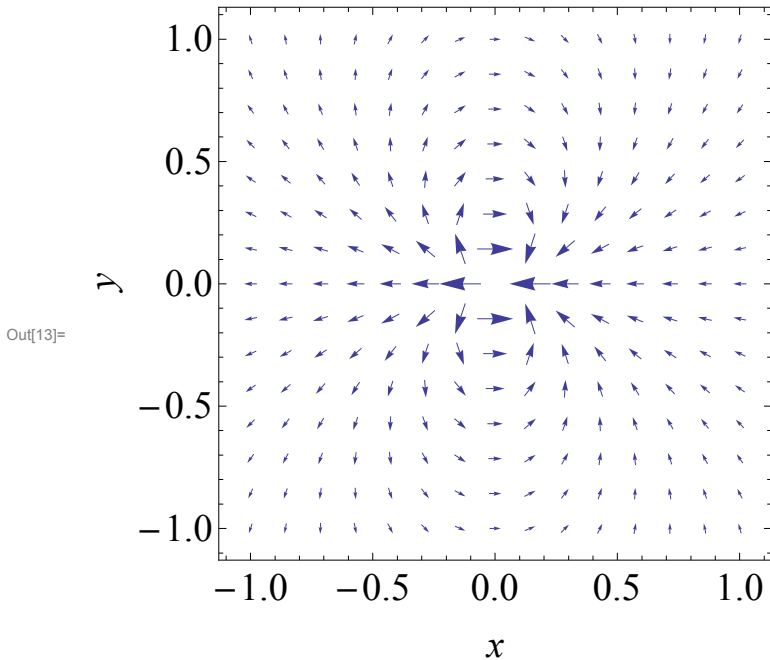


```
In[12]:= Plot3D[(* to avoid spurious at origin, y-coordinate was shifted slightly *)  
  GradF[x, y + 0.00001, 0] . {1, 0, 0}, {x, -1, 1}, {y, -1, 1},  
  BoxRatios -> 2, PlotRange -> {-10, 10}, ClippingStyle -> Opacity[0.5],  
  AxesLabel -> {x, y, z}, ImageSize -> 512,  
  BaseStyle -> {FontSize -> 20}, PerformanceGoal -> "Quality",  
  PlotPoints -> {101, 101}]
```

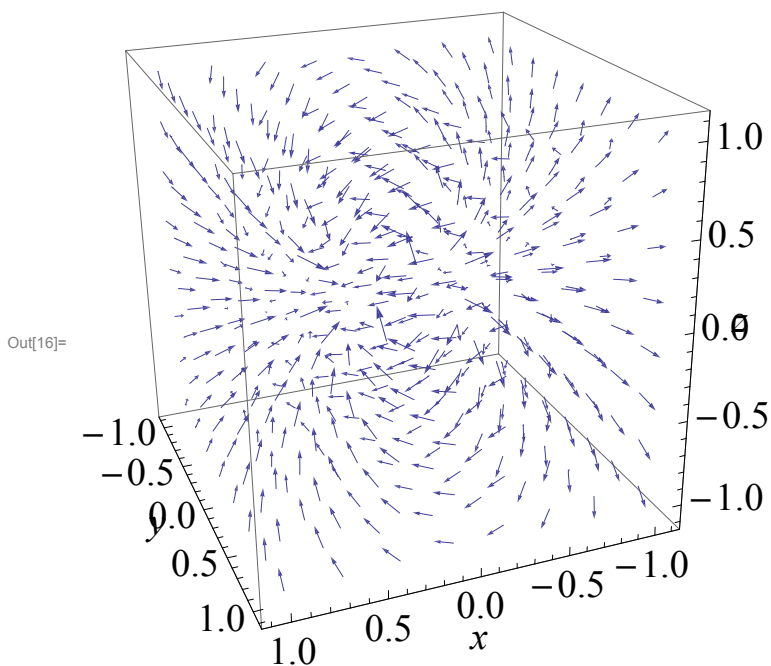
Out[12]=



```
In[13]= VectorPlot[
  Evaluate[D[GradF[x, y, 0] . {1, 0, 0}, {{x, y}}] ],
  {x, -1, 1}, {y, -1, 1}, (* #5 is Norm *)
  VectorScale -> {Small, Medium, If[#5 > 1000, 0, #5^0.2] &},
  BaseStyle -> {FontSize -> 20}, FrameLabel -> {x, y}]
```



```
In[16]= VectorPlot3D[
  Evaluate[D[GradF[x, y, z] . {1, 0, 0}, {{x, y, z}}] ],
  {x, -1, 1}, {y, -1, 1}, {z, -1, 1},
  VectorScale -> {Small, Small, If[#5 > 20, 0, #5^0.1] &},
  BaseStyle -> {FontSize -> 20}, AxesLabel -> {x, y, z}]
```



```

In[17]= Show[ (* Contour plot for constant electric field is added*)
  ContourPlot3D[Abs[GradF[x, y, z] . {1, 0, 0}] = {1/3, 1, 3},
    {x, -1, 1}, {y, -1, 1}, {z, -1, 1},
    ContourStyle -> Opacity[0.3], Mesh -> None,
    BaseStyle -> {FontSize -> 20}, AxesLabel -> {x, y, z}],
  VectorPlot3D[
    Evaluate[D[GradF[x, y, z] . {1, 0, 0}, {{x, y, z}}]],
    {x, -1, 1}, {y, -1, 1}, {z, -1, 1}, VectorStyle -> "Arrow3D",
    VectorScale -> {Medium, Medium, If[#5 > 20, 0, #5^0.1] &},
    VectorPoints -> {6, 4, 4},
    BaseStyle -> {FontSize -> 20}, AxesLabel -> {x, y, z}]]

```

Out[17]=

